

الوسائط المتعددة و برمجتها

السنة الثالثة

قسم تقنيات الحاسوب

المحاضرة الثالثة

إعداد

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## *Chapter 2*

# Digital Image Fundamentals

Digital Image Fundamentals

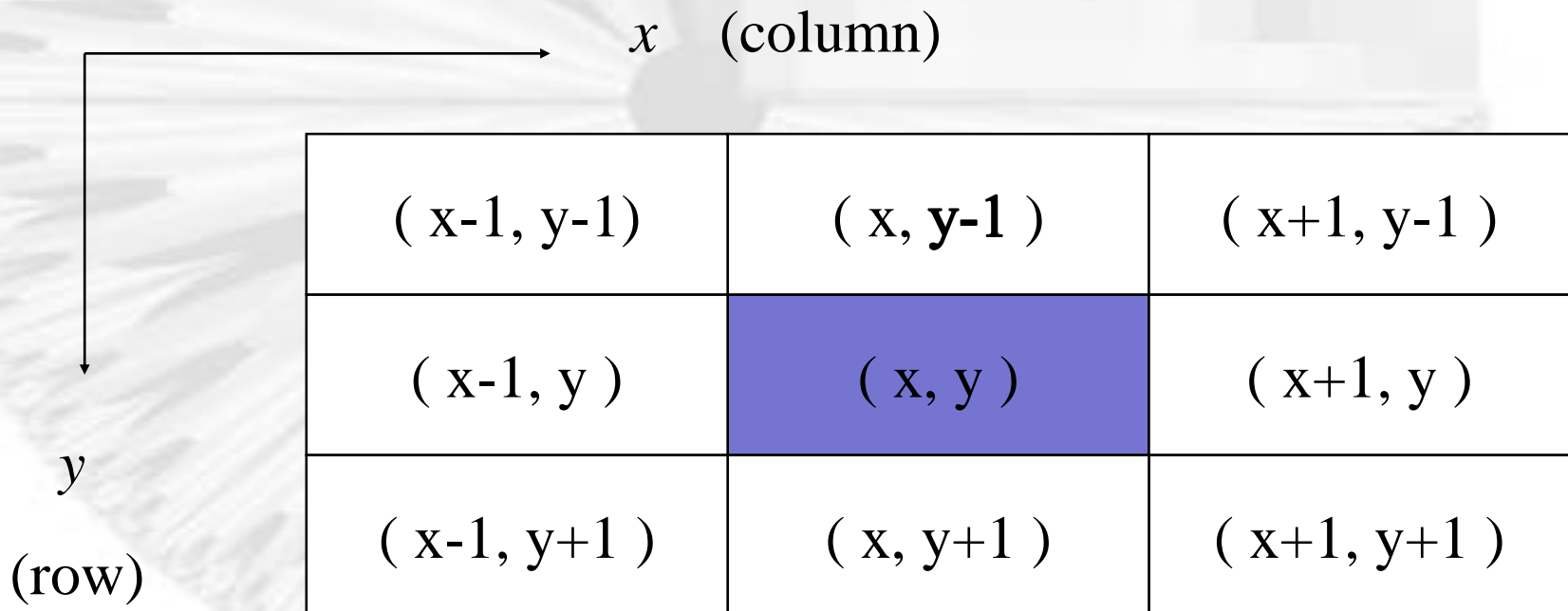
## 2.5 Some basic Relations Between Pixels:

- An image will be denoted by  $f(x,y)$ . when referring to a particular pixel, we lowercase letters, such as  $p$  and  $q$ . A subset of pixels of  $f(x,y)$  will be denoted be  $S$ .

# Neighbors of a pixel :

- a pixel **p** at coordinates **(x, y)** has the following neighbors:

**( x-1,y-1 ), ( x,y-1 ), ( x+1,y-1 ), ( x-1,y ) ( x+1,y ),  
( x-1,y+1 ), ( x,y+1 ), and ( x+1,y+1 )**



# 4-neighbors

- **4-neighbors of p**  $N_4(p)$  is the set of pixels, in horizontal and vertical neighbor have the coordinates:  
 $(x, y-1)$ ,  $(x-1, y)$ ,  $(x+1, y)$ , and  $(x, y+1)$ .
- **It is noted that** each of these pixels is a unit distance from  $(x, y)$  and also some of the neighbors of  $p$  will be outside the digital image if  $(x, y)$  is on the border of the image.

# *D-neighbors*

- **D-neighbors of p**  $D_4(p)$  is the set **The four diagonal neighbors of p have coordinates:**  
 $(x-1, y-1)$ ,  $(x-1, y+1)$ ,  $(x+1, y+1)$ ,  $(x+1, y-1)$
- **It is noted that** each of these pixels is a unit distance from  $(x, y)$  and also some of the neighbors of p will be outside the digital image if  $(x, y)$  is on the border of the image.
- and will be denoted by  $ND(p)$ . these points, together with the 4-neighbors are called the 8-neighbors of p, denoted by  $N8(p)$ .

# *8-neighbors*

- **8-neighbors of p**  $D_8(p)$  is the set **The eight neighbors of p that is:**
- $N_8(p) = N_D(p) + N_4(p)$ .
- **It is noted that** each of these pixels is a unit distance from  $(x, y)$  and also some of the neighbors of p will be outside the digital image if  $(x, y)$  is on the border of the image.

# *Adjacency, Connectivity, Regions, and Boundaries:*

- **The adjacent** pixels are the two pixels which are neighbor.
- **Connectivity between pixels** is an important concept used in establishing boundaries of objects and components of regions in an image.
- **To establish whether two pixels are connected :**
- we must determine if they are adjacent ( if they are neighbors ) and if their gray levels satisfy a specific criterion of similarity ( if they are equal ).
- **Example**, in binary image with values 0 and 1, two pixels may be 4-neighbors, but they are not said to be connected unless they have the same value.



# *Connectivity type*

Let  $V$  be the set of gray – level values to define connectivity, for example if only connectivity if pixels with intensities of 59, 60, and 61 is important, then  $V=\{59, 60, 61\}$ .

**We consider three types of connectivity:**

**4-connectivity.** Two pixels  $p$  and  $q$  with values from  $V$  are 4-connected if  $q$  is in the set  $N_4(p)$ .

**8-connectivity.** Two pixels  $p$  and  $q$  with values from  $V$  are 8-connected if  $q$  is in the set  $N_8(p)$ .

**$m$ -connectivity.** Two pixels  $p$  and  $q$  with values from  $V$  are  $m$ - connected if :

i-  $q$  is in the set  $N_4(p)$ , or

ii-  $q$  is in  $N_D(p)$  and the set  $N_4(p) \cap N_4(q)$  is empty. ( this is the set of pixels that are 4-neighbors of both  $p$  and  $q$  and whose values are from  $V$ ).

## *Problem 2.11*

Consider the two image subsets,  $S_1$  and  $S_2$ , shown in the following figure. For  $V=\{1\}$ , determine whether these two subsets are :

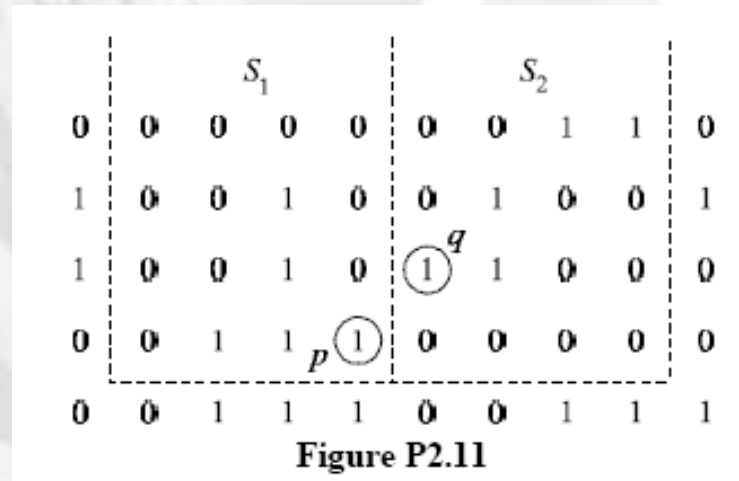
(a) 4-adjacent, (b) 8-adjacent, or (c) m-adjacent.

	$S_1$					$S_2$				
0	0	0	0	0	0	0	0	1	1	0
1	0	0	1	0	0	0	1	0	0	1
1	0	0	1	0	1	1	1	0	0	0
0	0	1	1	1	0	0	0	0	0	0
0	0	1	1	1	0	0	1	1	1	1

- NOTE**

**Two images  $S_1$  and  $S_2$  are adjacent if some pixel in  $S_1$  is adjacent to some pixel in  $S_2$ .**

# Solution



Let  $p$  and  $q$  be as shown in Fig. P2.11. Then,

- (a)  $S_1$  and  $S_2$  are not 4 connected **because**  $q$  is not in the set  $N_4(p)$ ;
- (b)  $S_1$  and  $S_2$  are 8 connected **because**  $q$  is in the set  $N_8(p)$ ;
- (c)  $S_1$  and  $S_2$  are  $m$  connected because (i)  $q$  is in  $N_D(p)$ , and (ii) the set  $N_4(p) \cap N_4(q)$  is empty.

## Problem 2.15

2.15 Consider the image segment shown.

- (a) Let  $V = \{0, 1\}$  and compute the lengths of the shortest 4-, 8-, and  $m$ -path between  $p$  and  $q$ . If a particular path does not exist between these two points, explain why.
- (b) Repeat for  $V = \{1, 2\}$ .

	3	1	2	1 ( $q$ )
	2	2	0	2
	1	2	1	1
( $p$ )	1	0	1	2

- (a) When  $V = \{0, 1\}$ , 4-path does not exist between  $p$  and  $q$  because it is impossible to get from  $p$  to  $q$  by traveling along points that are both 4-adjacent and also have values from  $V$ .

## Figure P2.15(a)

shows this condition it is not possible to get to  $q$ .

**The shortest 8-path** is shown in Fig. P2.15(b); its length is 4.

**The length of shortest  $m$ -path** (shown dashed) is 5. Both of these shortest paths are unique in this case.

**(b) One possibility for the shortest 4-path** when  $V = \{1; 2\}$  is shown in Fig. P2.15(c); its length is 6.

It is easily verified that another 4-path of the same length exists between  $p$  and  $q$ .

One possibility for the shortest 8path (it is not unique) is shown in Fig. P2.15(d)u its length is 4. The length of a shortest  $m$ -path (shown dashed) is 6. This path is not unique.

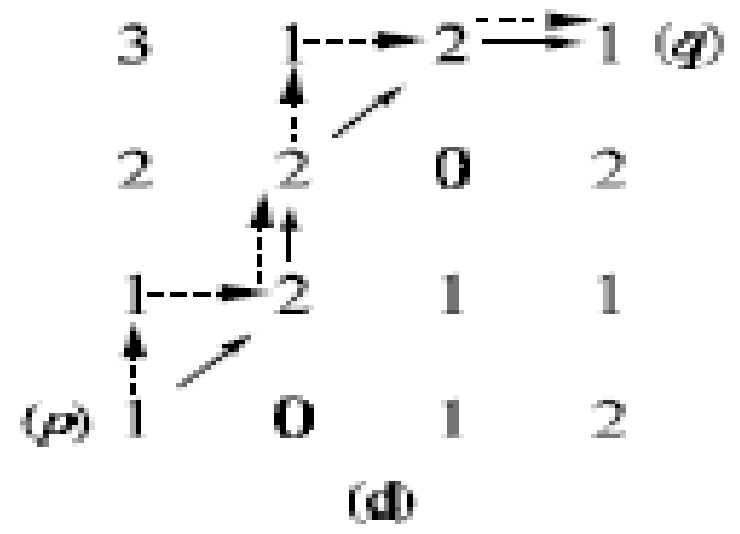
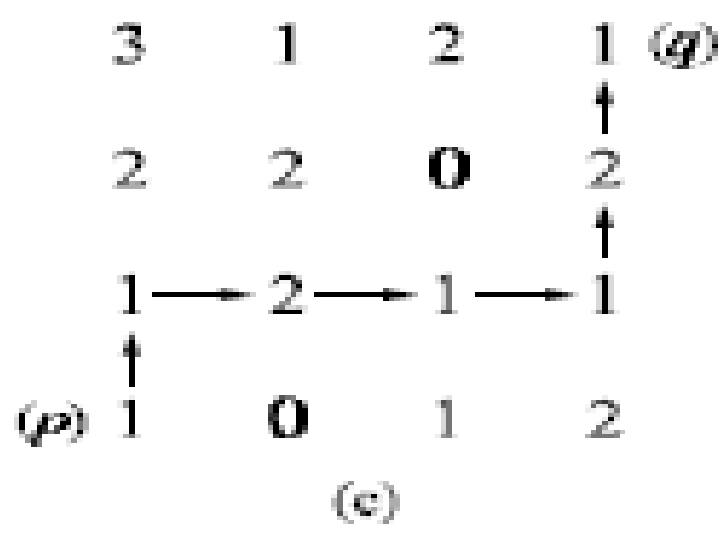
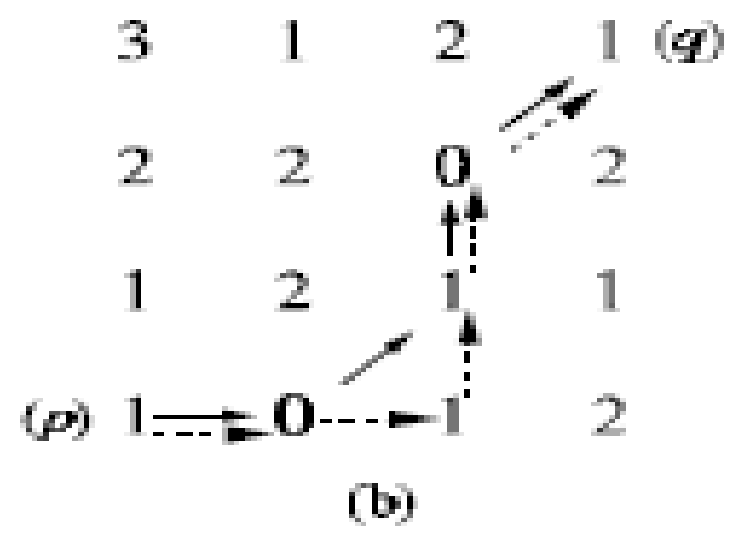
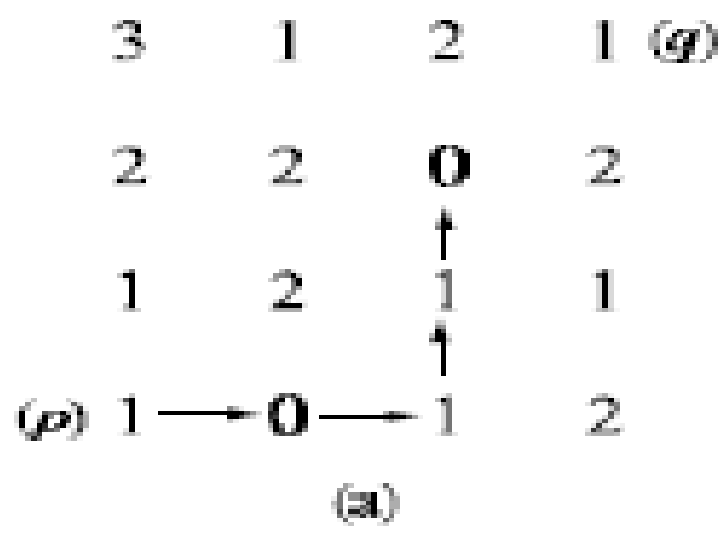


Figure P2.15