



الوسائط المتعددة و برمجتها

السنة الثالثة

قسم تقنيات الحاسوب

المحاضرة الرابعة

إعداد

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Chapter 2

Digital Image Fundamentals

Digital Image Fundamentals

Image Operations on a Pixel Basis

Numerous references are made to operations between images, such as **dividing** one image by another.

In some discussions, it is advantageous to use a more traditional matrix notation to denote a digital image and its elements:

$$\mathbf{A} = \begin{bmatrix} a_{0,0} & a_{0,1} & \cdots & a_{0,N-1} \\ a_{1,0} & a_{1,1} & \cdots & a_{1,N-1} \\ \vdots & \vdots & & \vdots \\ a_{M-1,0} & a_{M-1,1} & \cdots & a_{M-1,N-1} \end{bmatrix}. \quad (2.4-2)$$

In Eq. (2.4-2), images were represented in the form of matrices when we refer to an operation like “dividing one image by another,” we mean specifically that the division is carried out between *corresponding* pixels in the two images.

Image Operations on a Pixel Basis

Thus, for example, if f and g are images, the first element of the image formed by “dividing” f by g is simply the first pixel in f divided by the first pixel in g ; of course, the assumption is that none of the pixels in g have value 0.

Other arithmetic and logic operations are similarly defined between corresponding pixels in the images involved.

Image Combination

Arithmetic combination is applied on a pixel- by-pixel basis.

- The two images must have comparable dimensions.
- If not then image1 ($w_1 \times w_2$), image2 ($h_1 \times h_2$)
- The new image will have dimensions $w \times h$

$$w = \min (w_1 , w_2)$$

$$h = \min (h_1 , h_2)$$

•Two types of image combination:

•*arithmetic (image math)*

grayscale images



•*Logical (Boolean)*

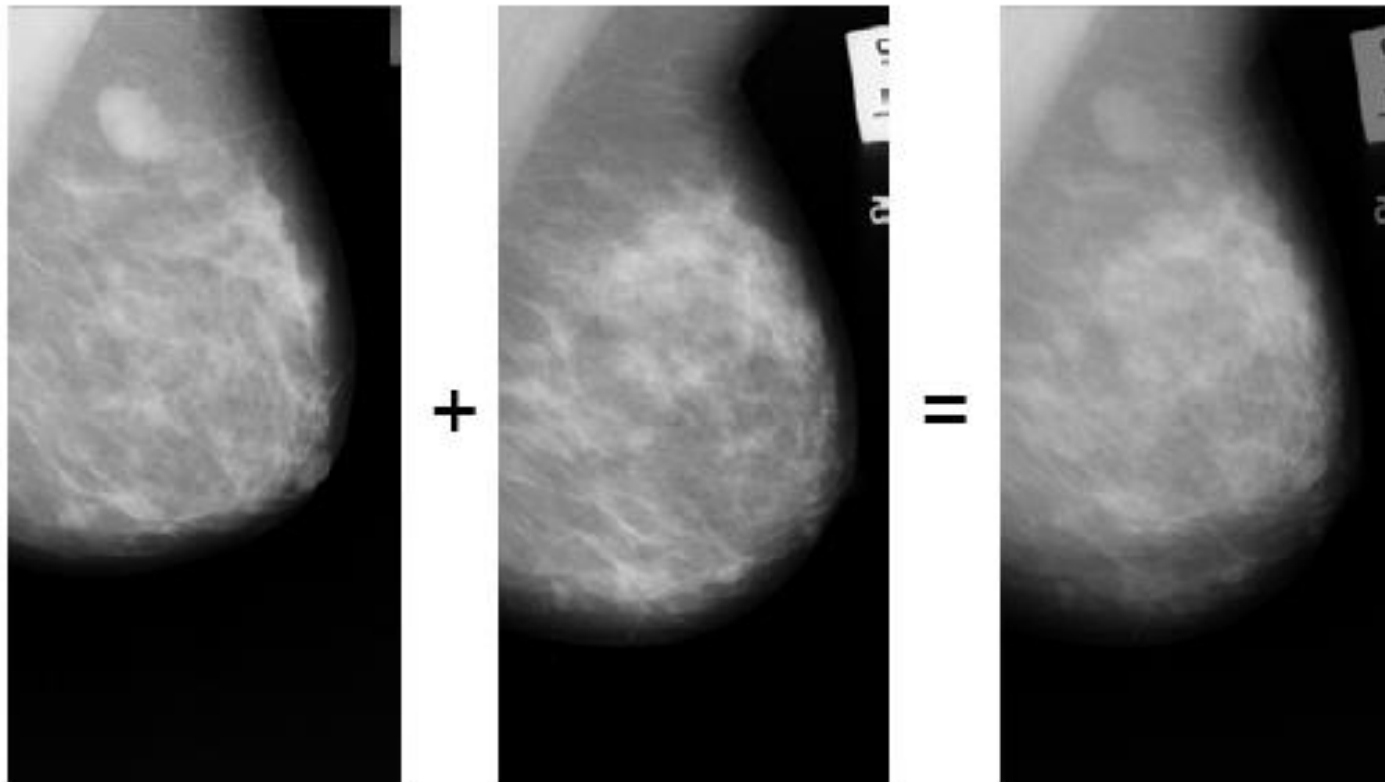
binary images



Image Addition

- Image addition superimposes information:
 - Pixels in the resulting image have values in the range 0-510.
 - Normalize the resulting image.divided by two (image averaging or converted to 16-bit.)
 - Primarily used for noise removal “Alpha blending”.
 - Give more emphasis to one image than the other
$$g(x,y) = \alpha f_1(x,y) + (1 - \alpha)f_2(x,y)$$
 - When $\alpha = 0.5$, $g(x,y)$ becomes a simple, even-weighted average.
 - Every pixel can have its own α stored in a separate α -channel.

Image Addition



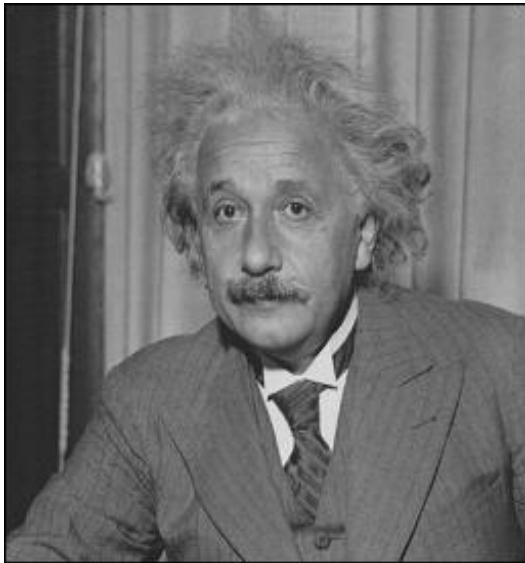


Image Subtraction

- **Image subtraction** calculates the differences between images
 - Used primarily for **change detection**
- Pixels in the resulting image have values in the range -255 to $+255$

$$g(x,y) = |f_1(x,y) - f_2(x,y)|$$

- Changes will be indicated by pixels in the **difference image** which have non-zero values.
 - The difference image will contain only features that change

Image Subtraction

- Sensor noise, slight intensity changes, and various other factors result in small differences which are of no significance.
- It is usual to apply a threshold to the difference image.
- Object motion can be measures through subtraction
 - e.g. track the motion of cells in response to chemical cues.

Image Subtraction

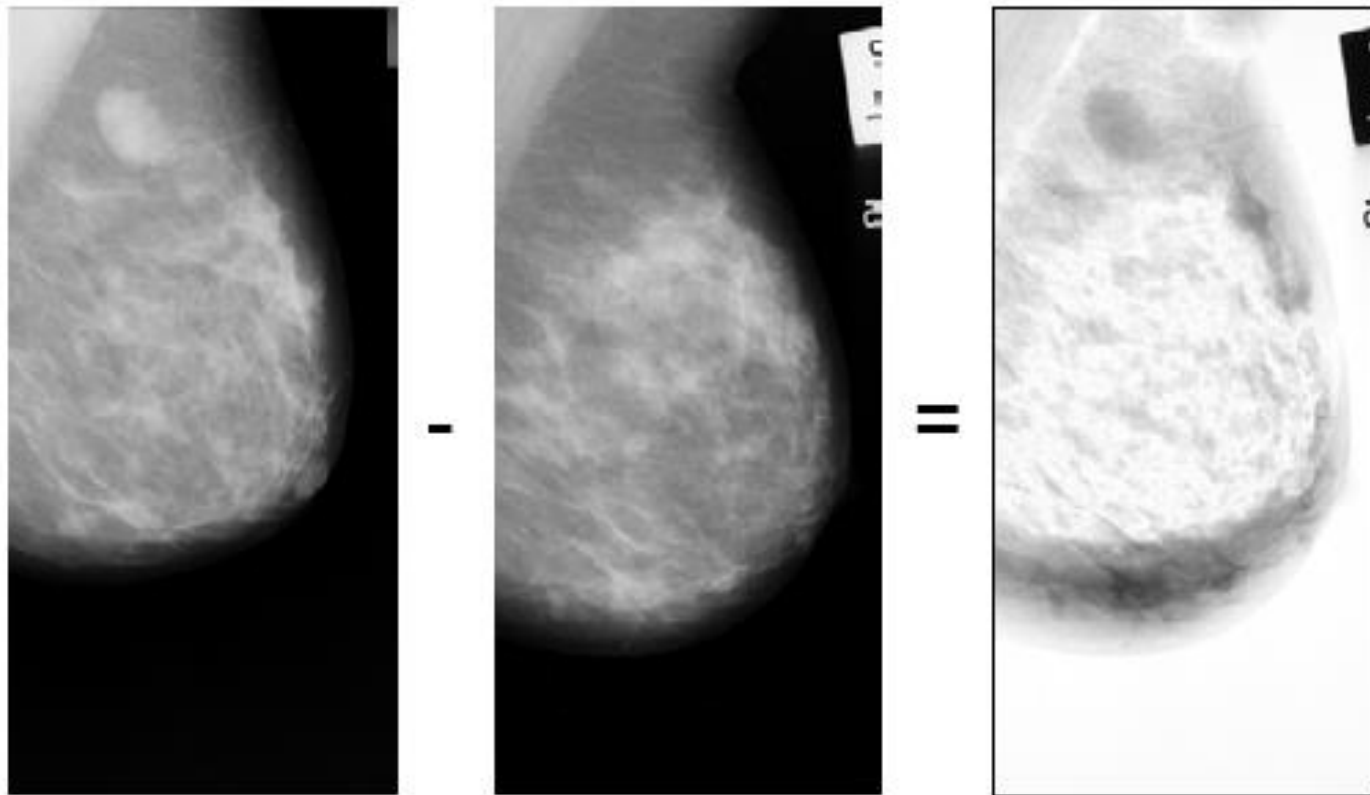


Image Division

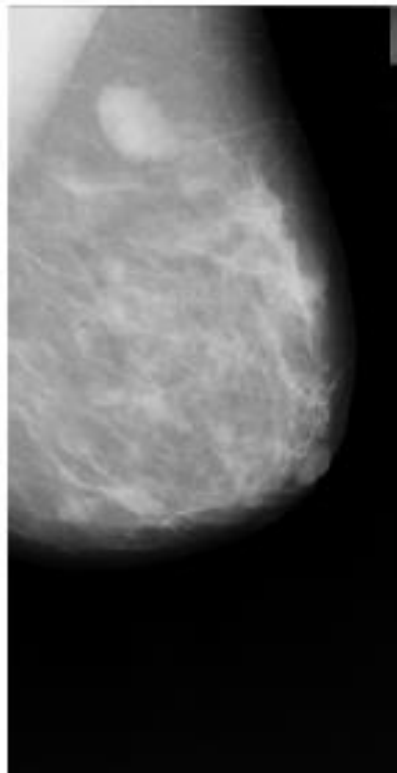
- **Image division** is used for removing backgrounds when linear detectors or cameras are used.
 - For meaningful results use floating-point arithmetic
 - Produces a ratio image in which the pixels should be rescaled and rounded \rightarrow normalise

$$g(x,y) = f_1(x,y)/f_2(x,y)$$

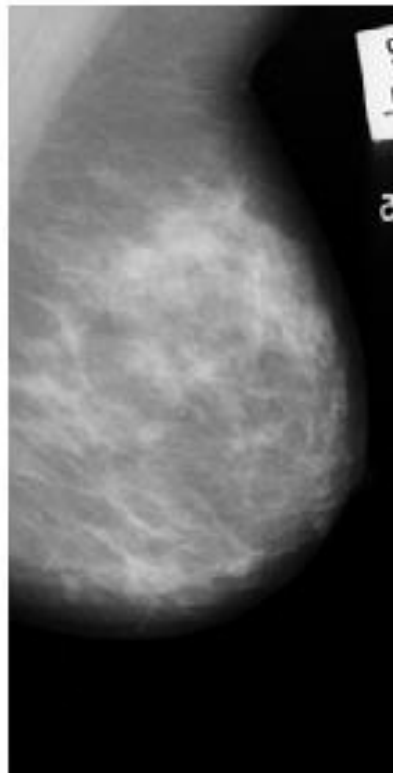
- Pixels of 0 intensity are removed from f_2 , adding a constant of unity to produce

$$f_2 \equiv f_2 + C, \quad C = 1$$

Image Division



\div



$=$



Image Multiplication

- Image multiplication is used for superimposing information

$$g(x,y) = f_1(x,y) \times f_2(x,y)$$

- Results in an extreme range of values: $0 \rightarrow 255$ becomes $0 \rightarrow 65,000$

- Loss of precision in rescaling

e.g. Combine edge and direction information from Sobel edge detection

e.g. Add fluorescence or other emission images to a reflection or transmission image

Image Multiplication

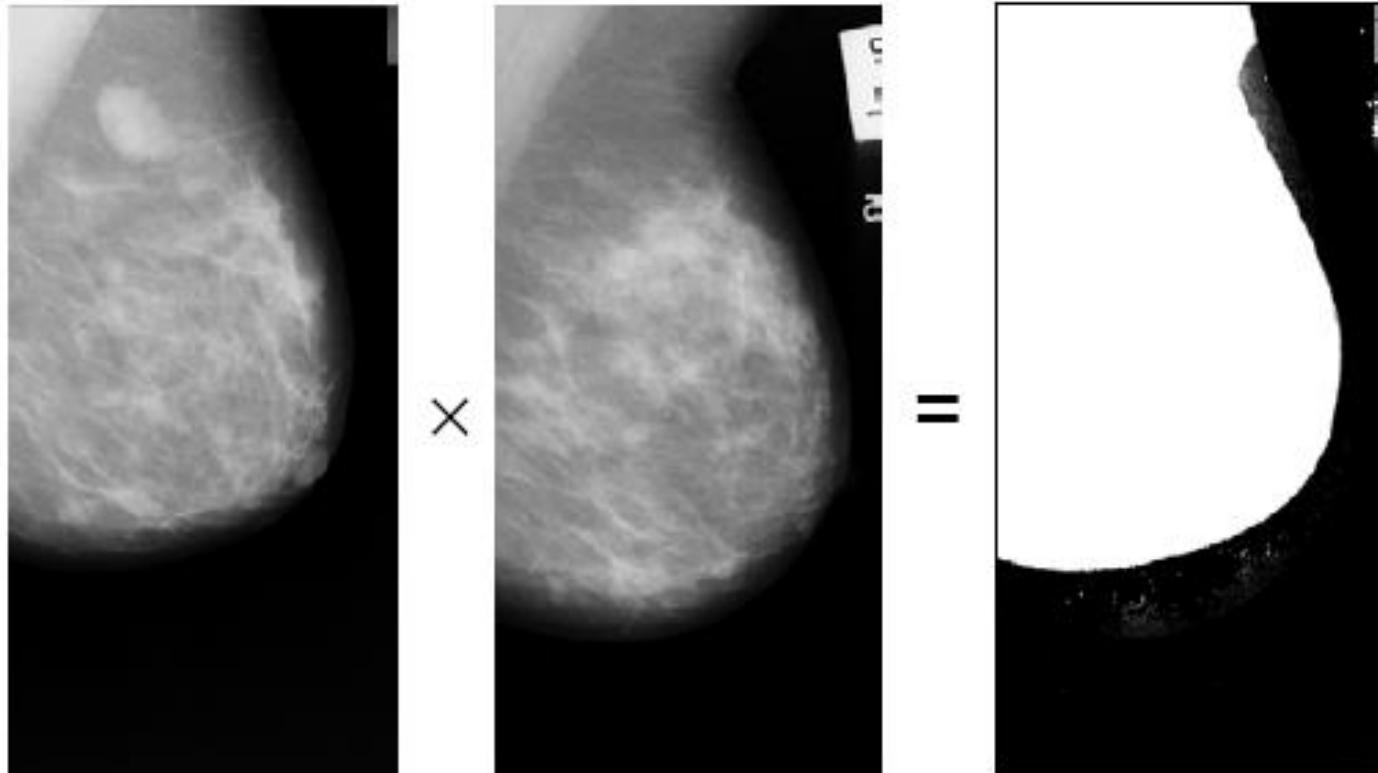


Image Minimum & Maximum

- Image combination using **min** (or **max**) involves retaining the darker (or lighter) intensity values at each location

$$g(x,y) = \min(f_1(x,y), f_2(x,y))$$

e.g. To build up a confocal scanning light microscope (CSLM) image with greater depth of field

Image Minimum

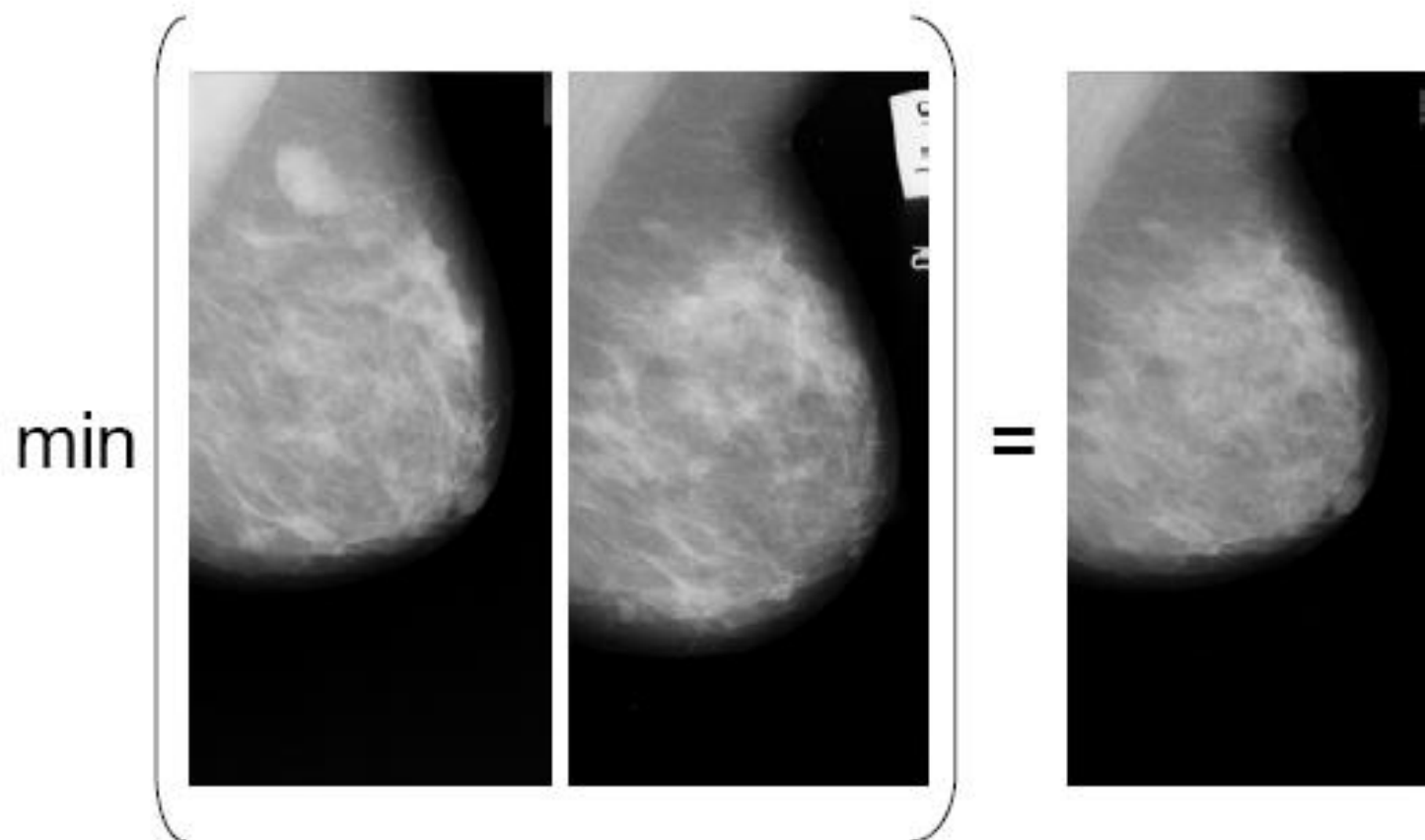
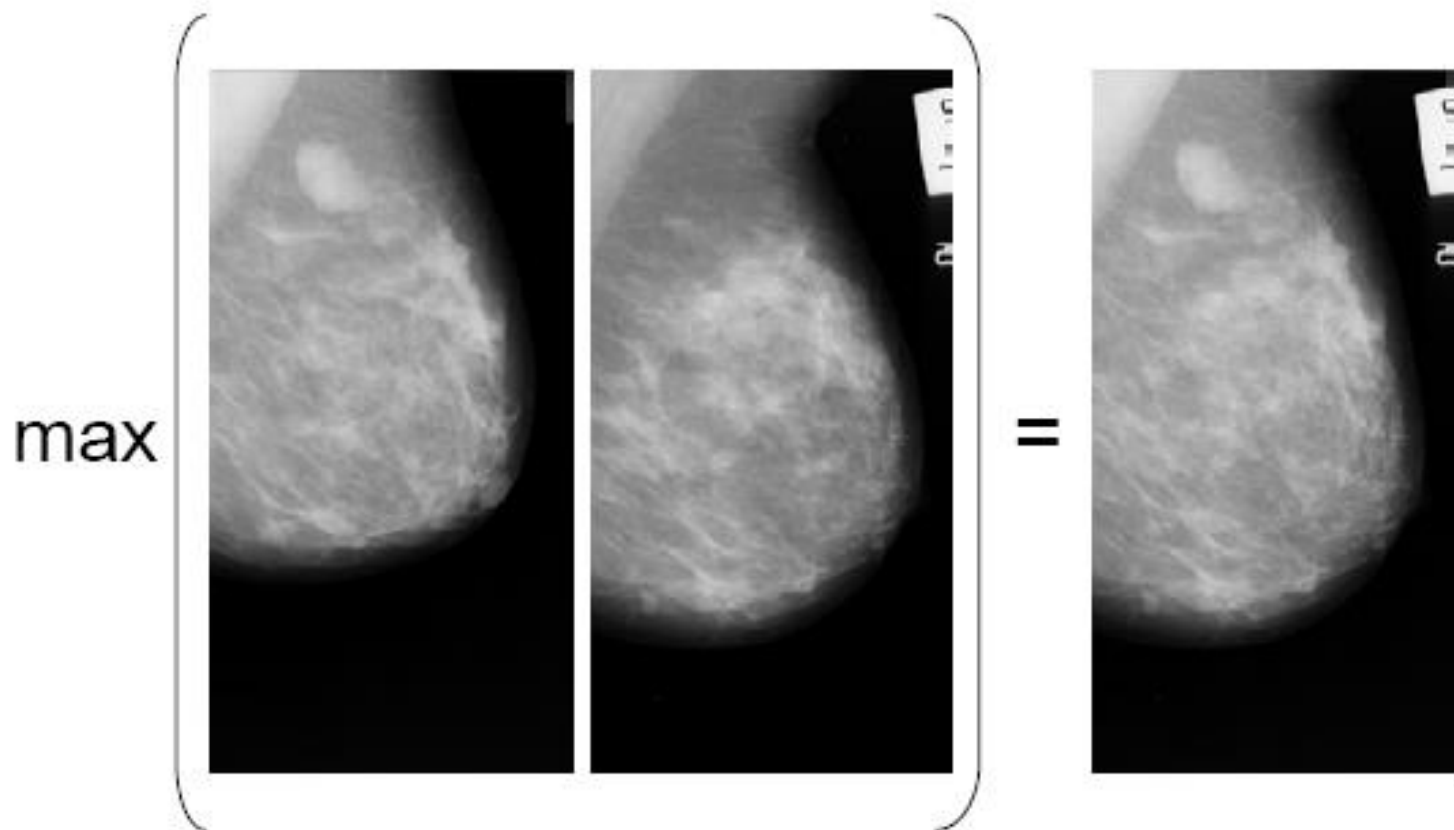
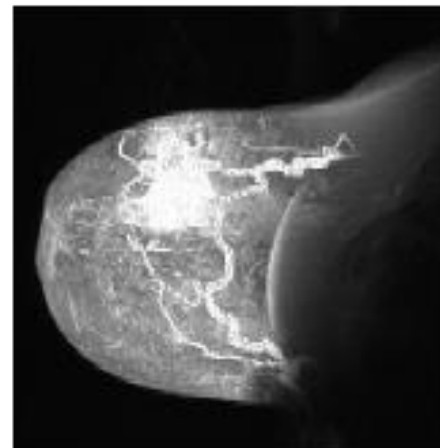
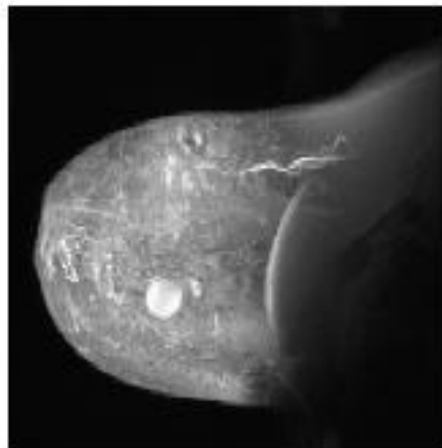


Image Maximum



Additional Effects

- Combining n images
 - **Shifting** each image slightly before performing combination, produces a perspective view of the surface.
 - Use the max function to combine images
 - e.g. maximum intensity projections



Logical Combination

- Logical or boolean combinations are usually applied to binary images

$$g(x,y) = f_1(x,y) \odot f_2(x,y)$$

- Operations
 - AND, OR, XOR, NOT

AND

- The pixel at location (x,y) is 1 if it is 1 in both images $f_1(x,y)$ and $f_2(x,y)$.
 - All pixels common to both images

$$g(x,y) = (f_1 \text{ AND } f_2) = 1$$
$$\text{if } f_1(x,y) = f_2(x,y) = 1$$

OR

- The pixel at location (x,y) is 1 if it is 1 in either of the images $f_1(x,y)$ or $f_2(x,y)$.

$$g(x,y) = (f_1 \text{ OR } f_2) = 1$$

if $f_1(x,y) = 1$ OR $f_2(x,y) = 1$

XOR

- Exclusive-OR
- The pixel at location (x,y) is 1 if it is 1 in either of the images $f_1(x,y)$ or $f_2(x,y)$, but not if it is 1 in both.

$$g(x,y) = (f_1 \text{ XOR } f_2) = 1$$

if $f_1(x,y) = 1$ AND $f_2(x,y) = 0$,
or $f_1(x,y) = 0$ AND $f_2(x,y) = 1$